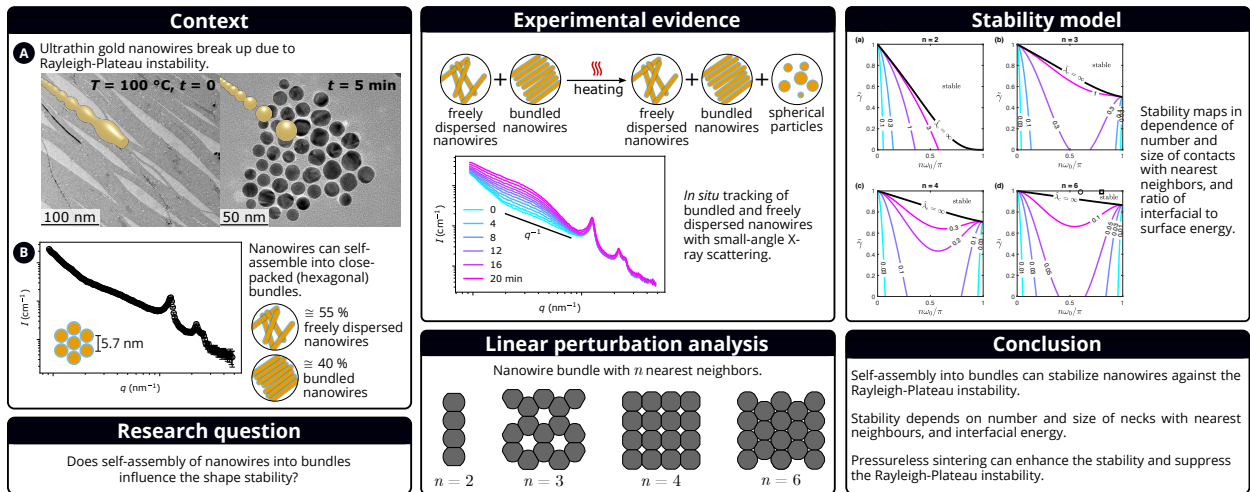


# Graphical Abstract

## Stabilization of ultrathin nanowires by self-assembly into bundles

Simon Bettscheider, Tobias Kraus, Norman A. Fleck



# Stabilization of ultrathin nanowires by self-assembly into bundles

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## Abstract

The relative tendency of freely dispersed and bundled gold nanowires to break up along their length by the Rayleigh-Plateau instability is investigated both experimentally and theoretically. Small angle X-ray scattering, in combination with transmission electron microscopy, reveal that the bundling of nanowires can enhance their stability. Theoretical support for this observation is provided by a linear perturbation analysis of a representative unit cell of bundled wires. A stability map is constructed for a bundle of nanowires to display the sensitivity of the Rayleigh-Plateau instability to the number and size of contacts with nearest neighbors per nanowire, and to the ratio of interfacial energy to surface energy. Stabilisation is enhanced by allowing the bundle of wires to sinter freely: a criterion for this kinetically-based stabilisation is given in terms of the ratio of pinch-off time for the instability to

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the sintering time to form the necks between nanowires.

*Keywords:* Rayleigh instability, nanowire, nanoparticle, diffusion, agglomeration

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## 1. Introduction

Ultrathin nanowires of length to diameter aspect ratio exceeding  $10^3$  are now readily available. They are prepared by chemically reducing a metal or semiconductor salt in the presence of an organic ligand [1]. The ligand directs one-dimensional growth of the nanowire by binding to the nanowire surface; additionally, the ligand stabilizes the nanowire core and the colloidal dispersion [2, 3, 4, 5, 6]. To date, ultrathin nanowires have been made from metals and their alloys (gold [7, 8, 9, 10, 3], iron-platinum [11], silver [12], ruthenium [13]) and semiconductors (copper sulfide [14], bismuth sulfide [15], antimony sulfide [16]). The nanowires are flexible and can spontaneously form continuous 2D and 3D superstructures; this tendency has been exploited to assemble opto-electronic devices [17, 18, 19]. Ultrathin nanowires have also been used in stretchable and optically transparent supercapacitors [17], in electrocatalytic membranes [20], and in the printed electrodes of bendable touchscreens [18].

A fundamental challenge for nanowire manufacture and use is their stability. Cylindrical wires are thermodynamically unfavorable in shape: a circular cylinder has a greater surface area, and consequently greater interfacial energy, than an array of spheres of the same overall volume, provided the ratio of the radius of spheres to that of the cylinder exceeds  $(3\pi/2)^{\frac{1}{3}}$  [21, 22]. This difference in surface energy drives the so-called Rayleigh-Plateau instabil-

22 ity [23, 24], also known as the morphological, geometric, shape, or Rayleigh  
23 instability. The evolution in shape of a circular cylindrical wire into spher-  
24 ical droplets by surface diffusion has been analyzed by Nichols and Mullins  
25 [21, 22]; the bulk of the wire is taken to be rigid and diffusional flow oc-  
26 curs in the axial direction along the surface of the wire. The time required  
27 for break-up is proportional to the fourth power of the cylinder radius so  
28 that thin wires are particularly prone to degradation [21, 22]. In practice,  
29 ultrathin gold nanowires in a dispersion fragment over a few weeks at room  
30 temperature, and over a few minutes at 100 °C.

31 Both energetic and kinetic considerations play a role in stabilizing nano-  
32 wires against the Rayleigh-Plateau instability [25]. Stabilization by energetic  
33 contributions can be enhanced by the presence of a substrate [26, 27, 28, 29],  
34 by anisotropy of the nanowire’s surface energy [30, 31, 32, 33], and by geo-  
35 metrical confinement in a matrix [34, 35, 36]. The addition of a ligand shell  
36 can enhance stability both energetically and kinetically [25]. For example,  
37 the ligand shell can reduce the nanowire’s surface energy and slow down  
38 diffusion [25, 37, 38, 34, 39, 40].

39 Surprisingly little is known about the stabilization of nanowires by their  
40 self-assembly into a bundle. Commonly, ultrathin nanowires are synthesized  
41 as colloids, and the resulting dispersion can comprise individual wires or  
42 wires that have self-assembled into close-packed bundles [1, 19, 41]. The  
43 size and relative density (also called packing density) of the bundles depend  
44 upon the choice of solvent [41], ligand type [40], and ligand shell density  
45 [42]. For example, the bundling of ultrathin gold nanowires (AuNWs) can  
46 be driven by a phase separation between the ligand shell and the solvent,

47 or by depletion forces induced by the solvent or unbound ligand molecules  
48 [43, 42]. Bundles also form when the nanowire dispersions are dried [44, 18].  
49 The center-to-center spacing of the wires ranges from 4.1 nm [43] to 5.9 nm  
50 [42], depending upon the method of self-assembly.

51 In the following, we show that the formation of bundles affects the shape  
52 stability of nanowires. The break-up of both fully dispersed and bundled  
53 nanowires is observed *in situ* by small-angle X-ray scattering. An analytical  
54 model is introduced to predict the influence of bundling upon shape stability.  
55 Stability maps are generated using a linear perturbation analysis, and are  
56 compared with the experimental results of the present study and with those  
57 reported in the literature.

## 58 **2. Experimental methods**

### 59 *2.1. Synthesis of ultrathin gold nanowires*

60 *Chemicals and materials.* All chemicals used are listed in Table S1 in the  
61 supplementary information.

62 *Synthesis.* Ultrathin gold nanowires (AuNWs) were synthesized using a pro-  
63 tocol based upon that of Feng et al. [45] and Nough et al. [40]. In a typical  
64 synthesis, 60 mg of the dry precursor  $\text{HAuCl}_4 \cdot n\text{H}_2\text{O}$  was placed in a glass  
65 vial and quickly covered with a volume of 9.9 mL of *n*-hexane; 2.04 mL of  
66 the ligand oleylamine was added while flushing with Ar. The mixture was  
67 vortexed for 5 min to dissolve the precursor. Finally, 3.06 mL of the reducing  
68 agent triisopropylsilane was added while flushing with Ar. The mixture was  
69 again vortexed for 30 s and the solution was rested, without stirring, at 25 °C  
70 for 24 h.

71 *Purification.* The reaction product was purified twice by adding two volumes  
72 of ethanol (30 mL each), centrifugating at 100 rcf for 1 min to precipitate the  
73 AuNWs, and redispersing in *n*-hexane after the first purification cycle and  
74 cyclooctane after the second purification cycle.

## 75 2.2. Heating of nanowires and *in situ* small-angle X-ray scattering

76 The break-up of nanowires was monitored *in situ* by small-angle X-ray scat-  
77 tering (SAXS). Samples for observation in SAXS were kept at room tem-  
78 perature for at least 16 h after purification before transferring them into  
79 glass capillaries with an inner diameter of 1.5 mm. To accelerate the break-  
80 up, the samples were heated *in situ* to either 60 °C or 70 °C. The heating  
81 stage was pre-heated to the desired temperature, and measurements were  
82 taken at 2 min intervals in the beamline of a Cu K $\alpha$  X-ray source (SAXS  
83 setup XEUSS 2.0, XENOCs, France). The scattered intensity was captured  
84 by a detector at a distance of approximately 1.2 m from the sample. The  
85 sample-to-detector distance was calibrated with a standard of silver behen-  
86 ate prior to each measurement. The two-dimensional scattering images were  
87 integrated (azimuthal integration) using the software Foxtrott (Synchrotron  
88 Soleil, France) to obtain scattering curves.

89 The (center-to-center) interwire distance  $d$  inside bundles of AuNWs was  
90 determined assuming Bragg scattering [46] using the formula

$$d = \frac{4\pi}{\sqrt{3}q_{uv}} \sqrt{u^2 + uv + v^2} \quad (1)$$

91 where  $q_{uv}$  is the value of the  $q$ -vector of the Bragg scattering peak of a two-  
92 dimensional hexagonal lattice of Miller indices  $u$  and  $v$  [46].

93 *2.3. Scattering model fits*

94 The volume fractions of gold in the form of bundled nanowires, freely dis-  
95 persed nanowires, and spherical particles in the dispersion were obtained by  
96 fitting a scattering model to the SAXS data. The model was based on the  
97 work of Sundblom et al. [47], Manet et al. [48], and Loubat et al. [19] and  
98 used the form factors of cylinders and spheres and the structure factor of crys-  
99 talline cylinders. Freely dispersed nanowires were modeled using the form  
100 factor of a cylinder convoluted with a Schulz-Zimm distribution to account  
101 for the distribution of their diameters. Bundles of nanowires were modeled  
102 by multiplying this form factor with the structure factor of a 2D hexagonal  
103 lattice. The structure factor was approximated by a sum of Lorentzian func-  
104 tions at the positions of the Bragg peaks. A Debye-Waller factor accounted  
105 for disorder in the 2D hexagonal lattice, for example caused by thermal  
106 fluctuations. Spherical nanoparticles were modeled by convoluting the form  
107 factor of spheres with a Schulz-Zimm distribution. All spherical particles  
108 (formed during the synthesis and during break-up) were consolidated in a  
109 single, broadly distributed function whose mean diameter was allowed to  
110 evolve with time. The overall scattered intensity was the volume-weighted  
111 sum of the scattered intensity of freely dispersed nanowires, bundled nano-  
112 wires, and spherical nanoparticles. Details on the model can be found in the  
113 supplementary information. The fits were implemented in Python using the  
114 library LMFIT [49].

115 *2.4. Transmission electron microscopy*

116 Small aliquots of the heated samples were prepared for *ex situ* observation by  
117 transmission electron microscopy. To this end, the aliquots were diluted to a

118 concentration of approximately  $[\text{Au}] = 0.05 \text{ mg/mL}$  and  $5 \mu\text{L}$  of the diluted  
119 sample was drop cast on a perforated carbon-coated grid (Plano, Germany).  
120 The perforated grid reduced drying artefacts when compared to standard  
121 carbon-coated grids. The samples were observed at an acceleration voltage  
122 of  $200 \text{ kV}$  in a JEM 2010 (JEOL, Japan) transmission electron microscope  
123 (TEM).

### 124 **3. Experimental results**

#### 125 *3.1. Ex situ transmission electron micrographs*

126 Ultrathin gold nanowires (AuNWs) were chemically synthesized using the  
127 protocol detailed above, dried on carbon-coated grids, and analyzed in a  
128 Transmission Electron Microscope (TEM). A typical micrograph (Fig. 1a,b)  
129 shows nanowires with uniform gold cores and diameters of  $1.6 \text{ nm}$  and a  
130 spacing of  $4.4 \text{ nm}$  that is caused by a monolayer of the ligand oleylamine  
131 on the metal. The length of the nanowires exceeded the field of view and  
132 was estimated to be above  $1 \mu\text{m}$ ; lengths of  $1$  to  $4 \mu\text{m}$  have been reported  
133 previously [50].

134 Heating of the AuNW dispersions to  $60 \text{ }^\circ\text{C}$  resulted in fragmentation of  
135 the nanowires. Samples that were kept at  $60 \text{ }^\circ\text{C}$  for  $10 \text{ min}$  contained an  
136 increased fraction of spheres (Fig. 1c,d) that further grew after  $20 \text{ min}$  at  
137  $60 \text{ }^\circ\text{C}$ , whereupon much of the micrograph was covered with spherical parti-  
138 cles (Fig. 1e,f).

139 The fragmentation of gold nanowires has been explained in terms of the  
140 Rayleigh-Plateau instability [39, 25]. Here, we are interested in the relative  
141 stability of bundled and freely dispersed wires. We used X-ray scattering



142 to quantify the volume fractions of intact and fragmented wires at elevated  
143 temperatures.

### 144 *3.2. In situ small-angle X-ray scattering*

145 Small-angle X-ray scattering (SAXS) from the AuNWs in cyclooctane at  
146 20 °C is shown in Fig. 2b. The scattered intensity depends on the shape  
147 of the particles (“form factor”) and their relative arrangement (“structure  
148 factor”) [46]. A dispersion of free AuNW has its scattering determined only  
149 by the form factor, as reported in [41, 42], for example.

150 Scattering from the samples used here (Fig. 2b) was dominated by the  
151 form factor for scattering vectors  $q < 1 \text{ nm}^{-1}$ , while the structure factor  
152 dominated for  $q > 1 \text{ nm}^{-1}$ . Hexagonally packed AuNW bundles caused dis-  
153 tinct peaks in the scattered intensity at  $1.27 \text{ nm}^{-1}$ ,  $2.20 \text{ nm}^{-1}$ , and  $2.52 \text{ nm}^{-1}$ .  
154 Such bundles have been reported previously [45, 19, 41]. They are caused by  
155 attractive, entropic interactions that are due to unbound ligands and linear  
156 solvent molecules that align between the wires [43, 42]. The peak positions  
157 indicate a center-to-center spacing of the wires of  $d = 5.7 \text{ nm}$ . Scattering  
158 models (discussed in the next section) revealed that the dispersion contained  
159 a fraction of approximately 55 % in dispersed nanowires and 40 % in nanowire  
160 bundles.

161 The fragmentation of wires through the Rayleigh-Plateau instability was  
162 initiated by heating the dispersion of wires and bundles to 60 °C and tracked  
163 via SAXS. Scattering measurements at 2 min intervals are shown in Fig. 2c.  
164 The scattered intensity initially scaled with  $q^{-1}$  in the region dominated by  
165 the form factor ( $q < 1 \text{ nm}^{-1}$ ), which is typical for cylindrical objects. The  
166 overall scattering in this region gradually increased, indicating the formation

167 of spherical particles. The overall scattering in the region dominated by  
168 the structure factor ( $q > 1\text{nm}^{-1}$ ) remained unchanged, indicating that the  
169 bundles did not fragment.

### 170 *3.3. Interpretation of scattering data*

171 The scattering model described in section 2.3 was used to extract quantitative  
172 volume fractions of the gold contained in dispersed nanowires, bundled nano-  
173 wires, and spherical particles from the time-dependent SAXS (Fig. 2d,e). The  
174 original gold volume fractions were  $54.8 \pm 1.8\%$  in freely dispersed nanowires,  
175  $40.4 \pm 1.2\%$  in bundled nanowires, and  $4.7 \pm 0.5\%$  in spherical nanoparti-  
176 cles. The fraction of gold in freely dispersed nanowires decreased linearly to  
177  $39.0 \pm 1.3\%$  over 20 min at  $60^\circ\text{C}$ , while that of spherical particles increased  
178 to  $21.2 \pm 0.3\%$ . This corresponds to a fragmentation rate of approximately  
179  $6.5\text{ km s}^{-1}\text{ mL}^{-1}$  of freely dispersed nanowires.

180 The volume fraction of bundled nanowires remained constant (Fig. 2e).  
181 Heating to  $70^\circ\text{C}$  led to the same qualitative results (Fig. S1 in the sup-  
182plementary information): freely dispersed nanowires broke up and bundled  
183 nanowires remained mainly intact. Note that an elevated temperature can  
184 induce the formation of bundles, too [42]. The formation and dissociation of  
185 bundles occurs over a time scales of hours [41], and is hence independent of  
186 the break-up that is observed over minutes.

187 The results of SAXS and TEM analysis, taken together, indicated the  
188 rapid fragmentation of dispersed AuNWs, but not of AuNWs in bundle form.  
189 We conclude that AuNWs stabilize each other in bundles. The following  
190 sections provide an analytical model for the stability of nanowires in bundles  
191 to provide additional insights into this observation.

192 **4. Analytical model for Rayleigh-Plateau instability of a bundle of**  
193 **nanowires**

194 The prototypical problem is sketched in Fig. 3, showing the progressive break-  
195 down of a cylindrical wire into discrete droplets. The wire resides in a vertical  
196 stack of fixed height and so the necks between neighboring wires can be ide-  
197 alized by fixed planes.

198 *4.1. Geometry*

199 A representative nanowire within a bundle is modeled as a circular cylinder  
200 of radius  $R$  truncated by  $n \geq 2$  flat surfaces, each representing the neck  
201 with a neighboring wire, as shown in Fig. 4. Values of  $n$  for tessellation are  
202  $n = 2, 3, 4, 6$ .

203 Our aim is to explore the possibility of diffusional flow of atoms along the  
204 surface of the wire in the axial direction in order to perturb the shape from  
205 prismatic to one where the cross-section varies with the axial coordinate  $z$ .  
206 Assume that the radius  $R(z, t)$  evolves with time  $t$  and varies harmonically  
207 with axial position  $z$ . Suppose that the radius of the cylinder is perturbed  
208 from the uniform reference state  $R = R_0$  to the state

$$R(z, t) = R_0 + \Delta R(t) + a(t) \cos(kz), \quad (2)$$

209 where  $a(t)$  is the perturbation amplitude,  $\lambda$  is the perturbation wavelength,  
210 and  $k = 2\pi/\lambda$  is the corresponding wavenumber (Fig. 5b). The term  $\Delta R(t)$   
211 results from the constraint that the cylinder maintains a constant overall  
212 mass. The shape (2) has the following interpretation. In general, assume  
213 that an initial imperfection exists at  $t_I = 0$ , and is of amplitude  $a(t_I = 0) > 0$

214 and wavelength  $\lambda$ . Our aim is to seek an expression for the rate of growth of  
 215 the imperfection  $\dot{a}(t)$ .

216 The evolution in shape of the wire occurs at fixed value of relative density  
 217 of the bundle of wires. Thus, the center-to-center spacing of adjacent wires  
 218  $2H$  is held constant, and the contact angle  $\omega(z, t)$  evolves with  $R(z, t)$  such  
 219 that

$$\cos \omega = \frac{H}{R}. \quad (3)$$

220 In the unperturbed reference state,  $R = R_0$ , the contact angle equals  $\omega_0$ ,  
 221 where  $\cos \omega_0 = H/R_0$ . Note that  $\omega$  is *not* the local contact angle as dic-  
 222 tated by local equilibrium of surface energies for the wire. Rather,  $\omega$  is a  
 223 macroscopic measure of the wire inclination at the edge of the contact. This  
 224 approximation has been justified by Parhami et al. [51] for the sintering of  
 225 a row of spherical particles. Example configurations for a bundle of wires  
 226 are shown in Fig. S2, and the relative density as a function of  $\omega_0$  is given in  
 227 Fig. S3 for the unperturbed state,  $a = 0$ . The perturbation analysis of the  
 228 present study builds upon that of Gill [28]; he considered the case of a single  
 229 wire on a surface, for which  $H$  is free to evolve with time.

#### 230 *4.2. Conservation of cylinder mass*

231 The term  $\Delta R(t)$  in (2) is determined from conservation of volume over the  
 232 wavelength  $\lambda$  as follows. The cross-section of the wire  $A_z^0$  in the unperturbed  
 233 state is

$$A_z^0 = \pi f_0 R_0^2, \quad (4)$$

234 where

$$f_0 \equiv 1 - \frac{n}{\pi} \left( \omega_0 - \frac{1}{2} \sin(2\omega_0) \right). \quad (5)$$

235 Consequently, the volume  $V_0$  of a length  $\lambda$  of the wire in the unperturbed  
 236 state is  $V_0 = A_z^0 \lambda$ . Now consider the perturbed state. The cross-sectional  
 237 area  $A_z$  of the cylinder at any axial position  $z$  is

$$A_z(z, t) = \pi f R^2, \quad (6)$$

238 where

$$f(\omega, n) \equiv 1 - \frac{n}{\pi} \left( \omega - \frac{1}{2} \sin(2\omega) \right). \quad (7)$$

239 Now write  $\omega(z) = \omega_0 + \Delta\omega(z)$  to give, via (3),

$$\Delta\omega = \left( \frac{\Delta R}{R_0} + \frac{a}{R_0} \cos(kz) - \frac{a^2}{R_0^2} \cos^2(kz) \right) \cot \omega_0 + \mathcal{O}(a^3). \quad (8)$$

240 We use (8) to re-write  $f(\omega, n)$  as

$$f(\omega, n) = f_0 - \frac{n}{\pi} \left( \Delta\omega(1 - \cos(2\omega_0)) + \Delta\omega^2 \sin(2\omega_0) \right). \quad (9)$$

241 Introduce the compact notation

$$\xi_1(\omega_0, n) \equiv \pi - n \left( \omega_0 - \frac{1}{2} \sin(2\omega_0) \right) = \pi f_0 \quad (10)$$

$$\xi_2(\omega_0) \equiv 1 - \cos(2\omega_0), \quad (11)$$

242 to write the current cross-sectional area  $A_z(z, t)$  as

$$A_z = \pi R_0^2 \left( f_0 + \frac{\Delta\omega}{\pi} (2\xi_1 \tan \omega_0 - n\xi_2) \right. \\ \left. + \frac{\Delta\omega^2}{\pi} (3\xi_1 \tan^2 \omega_0 - 2n\xi_2 \tan \omega_0 - n \sin(2\omega_0)) \right). \quad (12)$$

243 Conservation of volume dictates that the current volume of the cylinder over  
 244 one wavelength,  $V = \int_0^\lambda A_z dz$ , equals the volume  $V_0 = \pi R_0^2 f_0 \lambda$  in the un-  
 245 perturbed state, and consequently

$$\frac{\Delta R}{R_0} = \xi_3(\omega_0) \left( \frac{a}{R_0} \right)^2, \quad (13)$$

246 where

$$\xi_3(\omega_0, n) \equiv \frac{-\xi_1 + n\xi_2 \cot \omega_0 + n \sin(2\omega_0) \cot^2 \omega_0}{4\xi_1 - 2n\xi_2 \cot \omega_0}. \quad (14)$$

247 Note that  $\Delta R$  is  $\mathcal{O}(a^2)$ .

#### 248 4.3. Energetics: surface energy as driving force

249 The driving force for the Rayleigh-Plateau instability is the reduction in total  
 250 surface energy that accompanies growth of the perturbation. The interface  
 251 between neighboring wires possesses an interfacial free energy per unit area  
 252  $\gamma_c$ , and the free surface of the wire has a surface energy per unit area  $\gamma_s$ .

253 In the present study, the ligand shell is not considered separately. Effects  
 254 of the ligand shell can be incorporated by modifying the effective values of  
 255 surface energies and diffusivities. Effective values could be obtained from  
 256 advanced quantum chemical simulations [52]. Our earlier work showed how

257 such atomistic and molecular information can be incorporated into the effec-  
 258 tive surface energy and diffusivity values [25].

259 *4.4. Kinematics: shape evolution by surface diffusion*

260 The shape of each nanowire evolves by surface diffusion in the axial direction  
 261 [21, 22]. Conservation of mass requires that the surface divergence of the  
 262 surface diffusive flux  $\mathbf{j}$  and the normal velocity of matter deposited onto the  
 263 surface  $v_n$  sum to zero,

$$\nabla_s \cdot \mathbf{j} + v_n = 0, \quad (15)$$

264 where  $\nabla_s$  is the usual surface divergence operator, and a bold symbol denotes  
 265 a vector throughout this paper. Assume that the dominant surface flux is in  
 266 the axial direction and is of magnitude  $j$ . Then, (15) simplifies to

$$\frac{1}{R} \frac{\partial(Rj)}{\partial s} + v_n = 0, \quad (16)$$

267 where  $s$  is the arc length along the free surface (see Fig. 5b). The normal  
 268 velocity of matter deposited on the surface must equal the rate of change in  
 269 radius,  $v_n = \dot{R} = \dot{a} \cos(kz) + \mathcal{O}(a^2)$ . For small perturbations ( $a \ll R$ ), we  
 270 may write  $R^{-1} \partial(Rj)/\partial s \approx \partial j/\partial z$  for the derivative in (16). Consequently,  
 271 the surface flux  $j$  is

$$j = -\frac{\dot{a}}{k} \sin(kz) + \mathcal{O}(a^2). \quad (17)$$

272 **5. Linearised perturbation analysis**

273 *5.1. Stability map and critical wavenumber*

274 The presence of a perturbation changes the Gibb's free energy of the wire  
 275 over one wavelength  $\lambda$  by  $\Delta G$ , where

$$\Delta G = \gamma_s(A_s - A_s^0) + \gamma_c(A_c - A_c^0). \quad (18)$$

276 Here,  $A_s$  is the area of the free surface and  $A_c$  is the area at the constraining  
 277 neck over one wavelength, as shown in Fig. 5a. The superscript 0 denotes  
 278 the respective area in the unperturbed state.

279 The free surface area of the wire over one wavelength  $\lambda$  of the perturbation  
 280 is

$$A_s = \int_0^\lambda 2(\pi - n\omega)R \, ds. \quad (19)$$

281 For small perturbations, we can write

$$ds = \left( 1 + \frac{1}{2}(ak)^2 \sin^2(kz) + \mathcal{O}(a^4) \right) dz. \quad (20)$$

282 Now make use of (8) to obtain

$$A_s = A_s^0 \left( 1 + \left( \xi_3 \xi_4 + \frac{1}{4}(R_0 k)^2 \right) \frac{a^2}{R_0^2} \right), \quad (21)$$

283 where  $\xi_4$  is defined by

$$\xi_4(\omega_0, n) \equiv \frac{\pi - n\omega_0 - n \cot \omega_0}{\pi - n\omega_0} \quad (22)$$



284 and  $A_s^0 = 2(\pi - n\omega_0)R_0\lambda$  is the surface area of the free surface of the unperturbed cylinder. Note from (21) that  $(A_s - A_s^0)$  is second-order in  $a/R_0$ .

286 The contact area  $A_c$  over one wavelength is

$$A_c = 2n \int_0^\lambda R \sin \omega \, dz, \quad (23)$$

287 and can be re-written in terms of  $a/R_0$  by making use of the expression

$$\frac{\sin \omega}{\sin \omega_0} = 1 + \Delta\omega \cot \omega_0 - \frac{1}{2}\Delta\omega^2 + \mathcal{O}(\Delta\omega^3), \quad (24)$$

288 and by expressing the radius  $R$  in terms of  $\Delta\omega$  via (3), such that

$$\frac{R}{R_0} = 1 + \Delta\omega \tan \omega_0 + \Delta\omega^2 \tan^2 \omega_0. \quad (25)$$

289 Now make use of (8), along with (24) and (25) to express (23) as

$$A_c = A_c^0 \left( 1 + \xi_5 \frac{a^2}{R_0^2} \right), \quad (26)$$

290 where

$$\xi_5(\omega_0, n) \equiv \xi_3 + \xi_3 \cot^2 \omega_0 - \frac{1}{4} \cot^2 \omega_0 \quad (27)$$

291 and  $A_c^0 = 2nR_0\lambda \sin \omega_0$  is the contact area in the unperturbed, reference state over one wavelength. The result for  $A_c$  is also second-order in  $a/R_0$ .

293 Substitute the expressions (21) and (26) into the definition of Gibb's  
294 free energy change (18), and introduce the ratio of interfacial free energies

295  $\tilde{\gamma} = \gamma_c/\gamma_s$ , to obtain

$$\Delta G = \gamma_s A_s^0 \left( \frac{a}{R_0} \right)^2 \left( \xi_3 \xi_4 + \frac{1}{4} (R_0 k)^2 + \frac{\tilde{\gamma} \xi_5 n \sin \omega_0}{\pi - n \omega_0} \right). \quad (28)$$

296 The nanowire is stable against the formation of a perturbation of amplitude  
 297  $a$  and wavelength  $\lambda$  if  $\Delta G \geq 0$ . This is satisfied for wavelengths  $\lambda \leq \lambda_c$ ,  
 298 where the critical perturbation wavelength  $\lambda_c$  for which  $\Delta G = 0$  is given in  
 299 non-dimensional form by

$$\tilde{\lambda} \equiv \frac{\lambda_c}{2\pi R_0} = \frac{1}{2} \left( -\xi_3 \xi_4 - \frac{\tilde{\gamma} \xi_5 n \sin \omega_0}{\pi - n \omega_0} \right)^{-\frac{1}{2}}. \quad (29)$$

300 We note in passing that  $\xi_3 > 0$ ,  $\xi_4 < 0$ , and  $\xi_5 > 0$  and consequently  $\tilde{\lambda}$  is  
 301 real in (29). The wavenumber corresponding to  $\lambda_c$  is  $k_c = 2\pi/\lambda_c$ , and for  
 302 later use, we emphasize that the tilde over the symbol  $\lambda$  denotes the non-  
 303 dimensional quantity  $\tilde{\lambda} \equiv \lambda/(2\pi R_0)$ . The stability maps in Fig. 6 illustrate  
 304 (29) in graphical form, and show the sensitivity of  $\tilde{\lambda}_c$  to  $n$ ,  $\tilde{\gamma}$ , and  $\omega_0$ . It is  
 305 evident from Fig. 6 that a region ( $\tilde{\lambda}_c = \infty$ ) exists in the top-right of each  
 306 map for which the bundle is stable against break-up into discrete droplets.  
 307 Stability is enhanced by a large value of  $\tilde{\gamma}$ , a large value of  $\omega_0$  (corresponding  
 308 to a high relative density of the bundle), and by a small co-ordination number  
 309  $n$ . For reference, a free standing circular cylindrical wire is unstable for  
 310 all wavelengths exceeding  $\lambda_c = 2\pi R_0$ , as discussed by Nichols and Mullins  
 311 [21, 22]: thus,  $\tilde{\lambda}_c$  equals unity for the free standing wire.

312 *5.2. Perturbation growth rate and fastest growing perturbation*

313 We proceed to use the Cocks-Suo variational principle [53, 51, 28] to de-  
 314 rive the wavenumber of the fastest growing perturbation. The variational  
 315 functional is defined as  $\Pi(\dot{a}) = \Delta\dot{G}(\dot{a}) + \Psi(\dot{a})$ , where  $\Psi(\dot{a})$  is a dissipation  
 316 potential due to surface diffusion. A stationary value of  $\Pi$  with respect to  $\dot{a}$   
 317 gives the solution that satisfies the constitute law for surface diffusion,

$$\delta\Pi \equiv \delta(\Delta\dot{G}) + \delta\Psi = 0. \quad (30)$$

318 The variation in change of Gibb's free energy,  $\delta(\Delta\dot{G})$ , with respect to a  
 319 variation  $\delta\dot{a}$  is obtained from (28) as

$$\delta(\Delta\dot{G}) = \gamma_s A_s \left( \frac{2a\delta\dot{a}}{R_0^2} \right) \left( \xi_3 \xi_4 + \frac{1}{4}(R_0 k)^2 + \frac{\tilde{\gamma}\xi_5 n \sin \omega_0}{\pi - n\omega_0} \right). \quad (31)$$

320 The dissipation potential  $\Psi(\dot{a})$  is defined as

$$\Psi = \int_{A_s} \frac{j^2}{2\mathcal{D}_s} dA_s, \quad (32)$$

321 where  $\mathcal{D}_s = \delta_s D_s \Omega_s / (R_G T)$  is the surface diffusion constant,  $\delta_s$  is the thickness  
 322 over which surface diffusion occurs,  $D_s$  is the surface diffusivity,  $\Omega_s$  is the  
 323 molar volume of the wire material,  $R_G$  is the universal gas constant, and  
 324  $T$  is absolute temperature. To first order accuracy in  $a/R_0$ , we may write  
 325  $dA_s = R_0 d\varphi dz$ , so that (32) simplifies to

$$\Psi = \frac{nR_0}{\mathcal{D}_s} \int_0^\lambda \int_0^{\frac{\pi}{n} - \omega_0} j^2 d\varphi dz. \quad (33)$$

326 Now substitute the expression (17) for  $j$  into (33), and integrate to obtain

$$\Psi = \frac{\dot{a}^2 A_s^0}{4\mathcal{D}_s k^2}. \quad (34)$$

327 Upon making use of (31) and (34), the variational statement (30) reduces to

$$\frac{\dot{a}}{a} = -\frac{4\mathcal{D}_s \gamma_s}{R_0^4} (kR_0)^2 \left( \xi_3 \xi_4 + \frac{1}{4}(kR_0)^2 + \frac{\tilde{\gamma} \xi_5 n \sin \omega_0}{\pi - n\omega_0} \right) \quad (35)$$

328 for any assumed wavenumber  $k$ . The fastest growing perturbation has a  
 329 wavelength that maximizes  $\dot{a}$  in (35); by setting  $\partial(\dot{a}/a)/(\partial k)$  to zero, the  
 330 fastest growing wavelength is  $\lambda_{\max} = \sqrt{2}\lambda_c$ , where  $\lambda_c$  has already been defined  
 331 in (29). The wavenumber  $k_{\max}$  that corresponds to  $\lambda_{\max}$  follows immediately  
 332 as

$$k_{\max} = \frac{\sqrt{2}\pi}{\lambda_{\max}} = \frac{k_c}{\sqrt{2}}, \quad (36)$$

333 and the fastest growth rate  $(\dot{a}/a)_{\max}$  of the bundle at  $\lambda = \lambda_{\max}$  follows directly  
 334 from (35) as

$$\left( \frac{R_0^4}{\gamma_s \mathcal{D}_s} \frac{\dot{a}}{a} \right)_{\max} = (k_{\max} R_0)^4. \quad (37)$$

335 Note that the expression (36) for  $k_{\max}$  is the same as that derived previously  
 336 for the classical Rayleigh-Plateau instability of a single free-standing wire  
 337 [21, 22].

338 *5.3. Topology of wires after pinch-off*

339 The wavelength of the fastest growing imperfection  $\lambda_{\max} = \sqrt{2}\lambda_c$  is given by  
 340 (29) and can be written in the non-dimensional form  $\tilde{\lambda}_{\max} = \lambda_{\max}/(2\pi R_0) =$   
 341  $\sqrt{2}\tilde{\lambda}_c$ . The value of  $\tilde{\lambda}_{\max}$  dictates the asymptotic shape of the final, pinched-  
 342 off particles: (a) discrete sphere at small  $\tilde{\lambda}_{\max}$ , (b) truncated sphere at inter-  
 343 mediate  $\tilde{\lambda}_{\max}$ , and (c) rod at large  $\tilde{\lambda}_{\max}$ . Consider each in turn.

344 *(a) Discrete sphere*

345 A small value of  $\tilde{\lambda}_{\max}$  leads to break-up into an array of spherical droplets of  
 346 final radius  $R_s$ . Conservation of mass dictates that

$$\frac{R_s}{H} = \frac{1}{\cos \omega_0} \left( \frac{3}{2} \xi_1 \tilde{\lambda} \right)^{1/3}. \quad (38)$$

347 This geometry occurs provided  $R_s < H$ , and consequently  $\tilde{\lambda}_{\max} < \tilde{\lambda}_1$ , where

$$\tilde{\lambda}_1 \equiv \frac{2 \cos^3 \omega_0}{3 \xi_1} \quad (39)$$

348 upon suitable rearrangement of (38).

349 *(b) Truncated sphere*

350 Now consider the case  $\tilde{\lambda}_{\max} > \tilde{\lambda}_1$ . Then, the discrete droplets are truncated  
 351 spheres with flat circular necks between immediate neighbors, see Fig. 7a.  
 352 The height of each particle is  $2H$ , and its radius external to the necks is  $R_s$ .  
 353 The radius of each neck is  $R_s \cos \omega_s$ , where  $2\omega_s$  is the angle subtended by the  
 354 neck at the center of the particle. The radius  $R_s$  is related to  $R_0$  via the

355 identity from (3):

$$H = R_s \cos \omega_s = R_0 \cos \omega_0 \quad (40)$$

356 once  $\omega_s$  has been obtained from  $\omega_0$  by conservation of volume between the ref-  
 357 erence, unperturbed volume  $V_0$  and the final volume of the truncated sphere.  
 358 Routine algebra gives

$$V_0 = \xi_1 R_0^2 \lambda_{\max} = \frac{4}{3} \pi R_0^3 \xi_6 \cos^3 \omega_0, \quad (41)$$

359 where

$$\xi_6(\omega_s, n) \equiv (\cos \omega_s)^{-3} \left( 1 - \frac{n}{4} (2 + \cos \omega_s) (1 - \cos \omega_s)^2 \right). \quad (42)$$

360 A standard root-finding algorithm (“fzero” in Matlab R2021a) is used to solve  
 361 (41) and (42) for  $\omega_s$  in terms of  $(n, \omega_0, \tilde{\lambda}_{\max})$ . Truncated spheres are obtained  
 362 for an intermediate value of  $\tilde{\lambda}_{\max}$ . When  $\tilde{\lambda}_{\max}$  attains a transition value of  
 363  $\tilde{\lambda}_2$ , adjacent necks touch. This occurs at  $n\omega_s = 2\pi$ , and the associated value  
 364 of  $\xi_6(\omega_s = \frac{2\pi}{n}, n)$  is obtained from (42). Upon substitution into (41), we find

$$\tilde{\lambda}_2 = \frac{2 \cos^3 \omega_0}{3 \xi_1(\omega_0, n)} \xi_6 \left( \frac{2\pi}{n}, n \right). \quad (43)$$

365 In summary, truncated spheres are the pinched-off final shape when  $\tilde{\lambda}_1 <$   
 366  $\tilde{\lambda}_{\max} < \tilde{\lambda}_2$ .

367 (c) *Rods*

368 The discrete droplets adopt a rod-like shape for  $\tilde{\lambda}_{\max} > \tilde{\lambda}_2$ , as shown in  
369 Fig. 7a.

#### 370 5.4. *Pinch-off time*

371 Our linear perturbation analysis describes the initial stage of shape evolu-  
372 tion. It does not accurately capture the details of the nanowire pinch-off into  
373 discrete spheres. However, previous numerical calculations have shown that  
374 the initial perturbation growth rate is a good predictor for the pinch-off time  
375 [25]. Assume that a nanowire of initial perturbation amplitude  $a_I$  at time  $t_I$   
376 pinches off when the perturbation amplitude reaches a value  $a_p$  at time  $t_p$ .  
377 The pinch-off time  $t_p$  is related to the perturbation growth rate  $\dot{a}(t_I)$  via the  
378 approximation [25],

$$\ln\left(\frac{a_p}{a_I}\right) = \int_{t_I}^{t_p} \frac{\dot{a}(t')}{a} dt' \approx (t_p - t_I) \frac{\dot{a}}{a}(t_I). \quad (44)$$

379 By setting  $t_I = 0$  and inserting the fastest growth rate from (37), the pinch-off  
380 time is predicted as

$$\frac{\gamma_s \mathcal{D}_s t_p}{R_0^4} = (k_{\max} R_0)^{-4} \ln\left(\frac{a_p}{a_I}\right), \quad (45)$$

381 which is again consistent with the results obtained by Nichols and Mullins  
382 [22] for an isolated metal nanowire. Note that  $k_{\max} = 2\pi/\lambda_{\max}$  is directly  
383 related to  $k_c = 2\pi/\lambda_c$  via (36) and consequently  $k_{\max} = \sqrt{2}\pi/\lambda_c$ . Also  
384 recall that  $\tilde{\lambda}_c = \lambda_c/(2\pi R_0)$  is a function of  $(n, \tilde{\gamma}, \omega_0)$  as given by (29) and  
385 Fig. 6. Assume that all wavelengths of perturbation are present in the wire

386 so that the pinch-off time is dictated by the fastest growing perturbation  
 387 of wavelength  $\lambda_{\max} = \sqrt{2}\lambda_c$ . Thus, upon making use of (45), the pinch-  
 388 off time  $t_p$  scales as  $\tilde{\lambda}_c^4$ ; some broad conclusions can be deduced immediately  
 389 from Fig. 6. Consider a close-packed, fully triangulated arrangement of wires  
 390 ( $n = 6$ ), with  $\tilde{\gamma} < 0.8$ . Then, pinch-off is fastest for small contacts ( $\omega_0 \approx$   
 391 0) corresponding to low relative density and for large contacts ( $\omega_0 \approx \pi/6$ )  
 392 corresponding to almost vanishing porosity. A large drop in surface energy  
 393 from the surface value  $\gamma_s$  to the interfacial, contact value  $\gamma_c$  (that is, a small  
 394 value of  $\tilde{\gamma} \equiv \gamma_c/\gamma_s$ ) leads to a faster pinch-off.

395 The formula (45) also applies to the case of a free-standing wire, with  
 396  $k_{\max} = \sqrt{2}\pi/\lambda_c$  and  $\lambda_c = 2\pi R_0$ , such that  $\tilde{\lambda}_c = 1$ . Thus, the plots of Fig. 6  
 397 can be used immediately to determine whether bundling reduces or increases  
 398 pinch-off time. In broad terms, a bundle of wires is more stable than the  
 399 isolated wire in regimes of the map for which  $\tilde{\lambda}_c > 1$ .

## 400 6. Discussion

### 401 6.1. Comparison of experiment and perturbation analysis

402 The experiments reported above indicate that a bundle of ultrathin gold  
 403 nanowires fragments more slowly than freely dispersed nanowires. Our per-  
 404 turbation analysis shows that stabilization arises from the presence of necks  
 405 between wires. Whether stabilization occurs or not depends upon the num-  
 406 ber of necks  $n$ , surface energy ratio  $\tilde{\gamma}$ , and initial contact angle  $\omega_0$  as shown  
 407 in the stability maps of Fig. 6. It is instructive to make use of the material  
 408 properties and geometric parameters of the present experimental study in  
 409 order to assess whether the predictions match the observed stabilization due



410 to bundle formation.

411 The measured radius of gold nanowires was approximately 0.84 nm and  
412 the thickness of the ligand shell was 2.2 nm [54, 55]. The AuNWs formed  
413 fully-triangulated bundles with  $n = 6$  and a center-to-center distance of  
414 5.7 nm, giving  $\omega_0 \approx \pi/10$ . The surface energy  $\gamma_s$  is set by the interaction  
415 between ligand and solvent molecules, and the interfacial energy  $\gamma_c$  by the  
416 interaction of ligand shells. The spacing indicates that solvent was always  
417 present between the ligand shells, implying  $\tilde{\gamma} \approx 1$ . These parameters put  
418 the system at the operating point  $(n, \tilde{\gamma}, n\omega_0/\pi) \approx (6, 1, 0.6)$  in the maps  
419 of Fig. 6, inside a region of unconditional stability. This explains why the  
420 bundled AuNWs were observed to be more stable than the freely dispersed  
421 ones.

422 Nouh et al. [40] exchanged the ligand oleylamine with trioctylphosphine  
423 and observed that the wires' stability increased, but did not provide an  
424 explanation for this finding. It was not stated whether stabilization was  
425 due to the different bond chemistry, the steric properties of the ligands,  
426 or the tighter bundling at an interwire distance of 3.75 nm [40]. We lo-  
427 cate their material and geometric parameters to be at the operating point  
428  $(n, \tilde{\gamma}, n\omega_0/\pi) \approx (6, 1, 0.8)$  in Fig. 6 in a region of unconditional stability,  
429 consistent with their experimental observations.

### 430 *6.2. Comparison of pinch-off time and free sintering time*

431 The analysis of the Rayleigh-Plateau pinch-off instability of a bundle of wires  
432 assumes that the center-to-center spacing of the wires remains constant, with  
433 the instability driven by surface diffusion in the axial direction. In addition,  
434 free sintering can occur such that the bundle of wires densifies by in-plane

435 surface diffusion, and the center-to-center spacing of neighboring nanowires  
 436 reduces. It is instructive to obtain an expression for the sintering time  $t_s$  to  
 437 achieve a given contact size  $c$  between adjoining wires, and to compare this  
 438 sintering time with the pinch-off time  $t_p$  for this same value of  $c$ . Sintering  
 439 stabilizes against pinch-off when  $t_s$  is less than  $t_p$ . Alternatively, when  $t_s$   
 440 exceeds  $t_p$  the Rayleigh-Plateau instability occurs with break-up of the wires  
 441 into discrete particles.

442 The sintering time  $t_s$  is calculated as follows. We focus attention on  
 443 the early stages of sintering involving initial neck formation and neck growth  
 444 (stage I sintering) [56, 51]. Consider a row of cylinders with an initial contact  
 445 length  $c = 0$  (see Fig. A.1). Sintering increases  $c$  and decreases  $H$ , as shown  
 446 in Fig. A.1. We follow Parhami et al. [51] and determine, for the 2D plane  
 447 strain case, the dependence of  $c$  upon sintering time  $t_s$ , such that

$$c^6 = \frac{81}{2} \mathcal{D}_c R_0^2 (2\gamma_s - \gamma_c) t_s. \quad (46)$$

448 Here,  $\mathcal{D}_c$  is the diffusion constant in the contact zone (grain boundary). The  
 449 derivation is given in Appendix A.

450 The sintering time  $t_s$  to achieve a neck size  $c$  is compared in Fig. 8 with  
 451 the pinch-off time  $t_p$  for the same value of  $c$ , for selected values of  $\tilde{\gamma}$  and  
 452  $\tilde{D} = \mathcal{D}_c/\mathcal{D}_s$ . Sintering is sufficiently fast to stabilize the nanowire shape at  
 453 large  $\tilde{\gamma}$  and large  $\tilde{D}$ . These conditions are typically satisfied for metals, for  
 454 which  $\tilde{\gamma} \approx 0.3$  to  $0.4$  [57] and  $\tilde{D} \approx 10^{-3}$  to  $10^{-1}$  [58]. Note that, for the  
 455 choice  $\tilde{\gamma} = 0.1$  and  $\tilde{D} = 10^{-5}$ , pinch-off is anticipated at  $c/R_0 \approx 0.1$  since  
 456  $t_p = t_s$  at this value of contact size between neighboring wires.

457 A critical neck size  $c_c$  can be defined for which  $t_s = t_p$ . Then, the sintering

458 time is smaller than the pinch-off time for  $c < c_c$ . For  $c > c_c$ , the instability is  
459 faster than sintering and the wires break up into discrete droplets. Contours  
460 of  $c_c$  are plotted in Fig. 9:  $c_c$  increases with increasing relative diffusivity  $\tilde{D}$ .  
461 For sufficiently large  $\tilde{D}$ , sintering is always faster than pinch-off and thereby  
462 stabilizes the wire.

## 463 7. Concluding remarks

464 Ultrathin nanowires can self-assemble into bundles. *In situ* SAXS and *ex situ*  
465 TEM reveal that bundling delays the Rayleigh-Plateau instability. An ana-  
466 lytical model, based on interfacial energy, geometrical confinement and axial  
467 surface diffusion, indicates that bundle formation can render the nanowire  
468 unconditionally stable. Stability depends upon the number and size of necks  
469 between neighboring wires, and upon the surface and interfacial energies. An  
470 optimal neck size maximizes pinch-off time for packings with more than two  
471 neighbors.

472 Pressureless sintering, in its early stages, is much more rapid than the  
473 rate of pinch-off by the Rayleigh-Plateau instability. However, the rate of  
474 sintering decreases sharply with increasing time,  $\dot{c} \propto t^{-5/6}$  as given directly  
475 from (46), and consequently the Rayleigh-Plateau instability may ensue.

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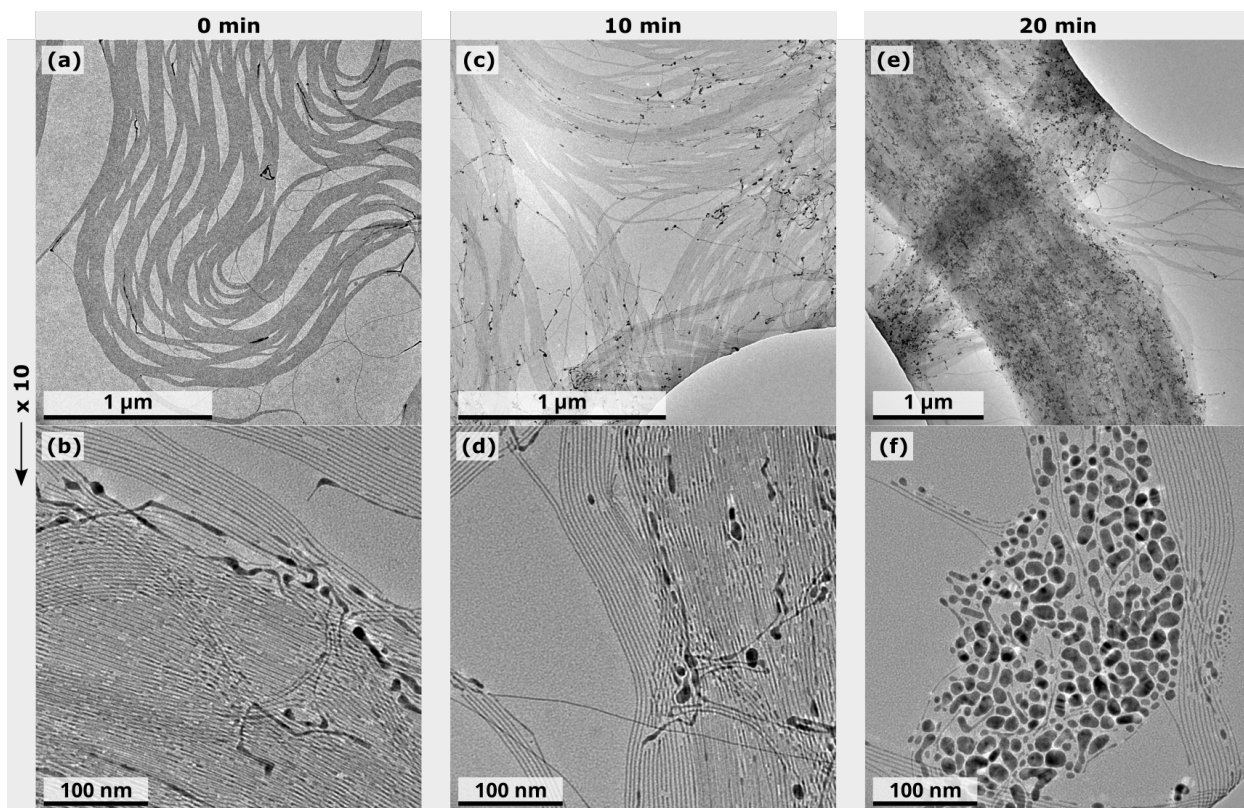


Figure 1: Transmission electron micrographs of ultrathin gold nanowires after drying at room temperature (a) and (b); and after heating them to 60 °C for 10 min (c) and (d); and 20 min (e) and (f). The wires fragmented into spherical particles.

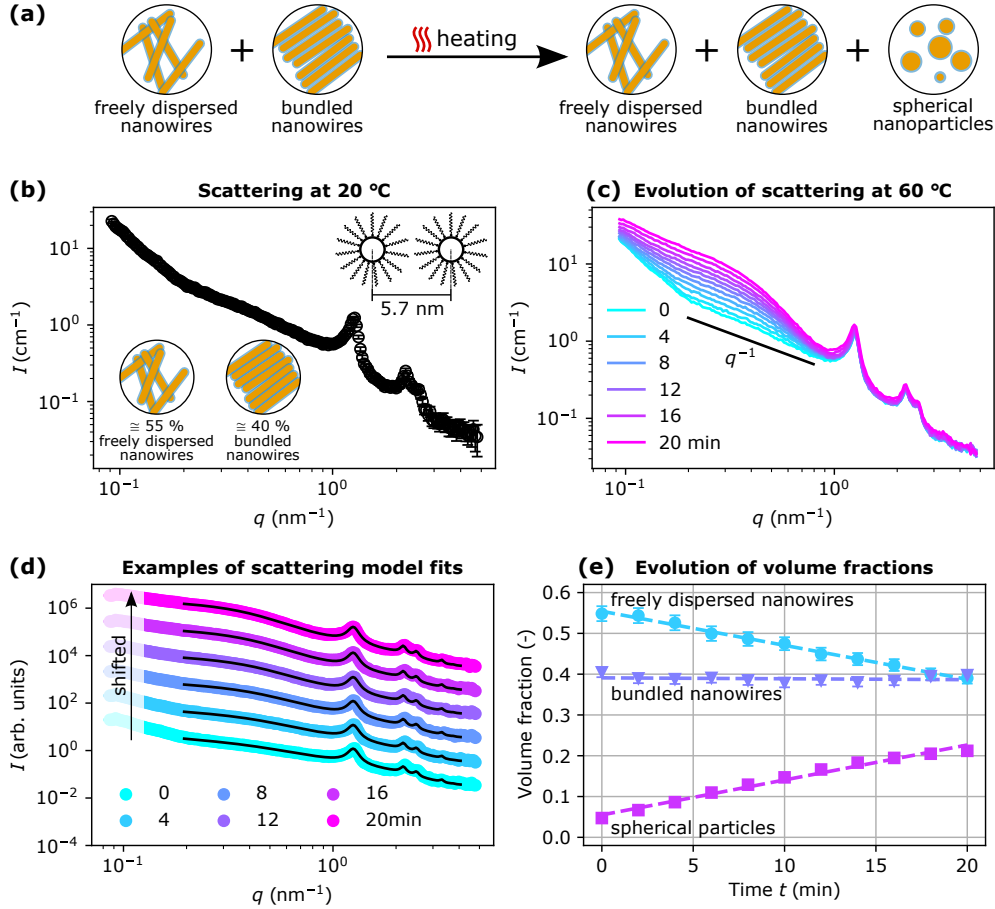


Figure 2: Analysis of nanowire shape stability via X-ray scattering. **(a)** The fragmentation of wires was induced by heating a dispersion to 60 °C and was observed via *in situ* Small-Angle X-ray Scattering (SAXS). **(b)** Distinct scattering maxima indicate that 40% of the gold existed in bundles and 55% in dispersed nanowires. The remaining 5% were in spherical nanoparticles, a by-product of the synthesis. The interwire (center to center) distance inside the bundles was 5.7 nm. **(c)** Heating to 60 °C increased scattering at small  $q$ -values, indicating the formation of spheres. **(d)** Scattering models (solid lines) were fitted to the scattering (dots) at selected times to quantify the change in volume fractions. The scattering curves are shifted vertically for better visualization. **(e)** Volume fractions of gold in freely dispersed nanowires, bundled nanowires, and spherical particles from the scattering models. Error bars denote the standard errors of the fits. The dashed line are linear fits.

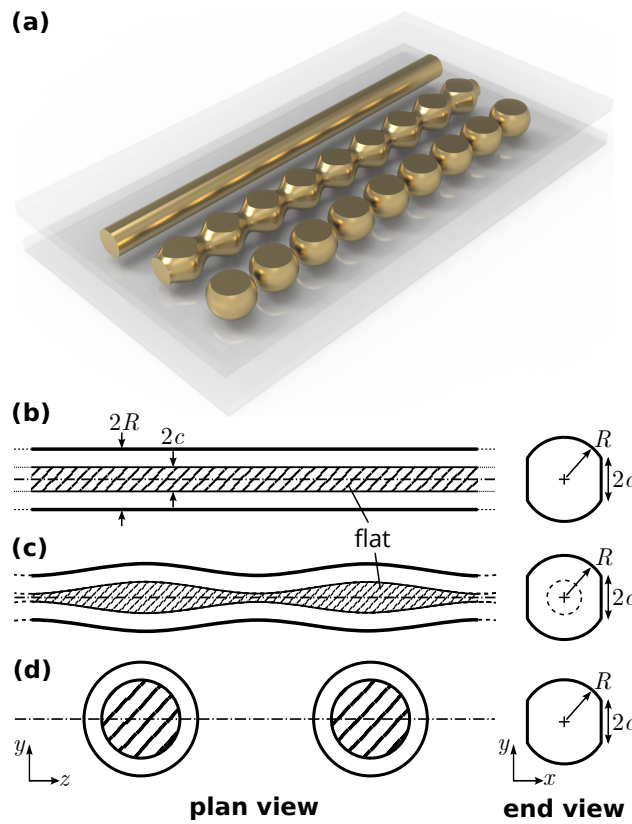


Figure 3: The prototypical problem showing a stacked nanowire. (a) Rendered view of three states. The nanowire may remain (b) prismatic in shape (stable), or it may evolve into (c) a non-uniform shape and thence to (d) discrete droplets.



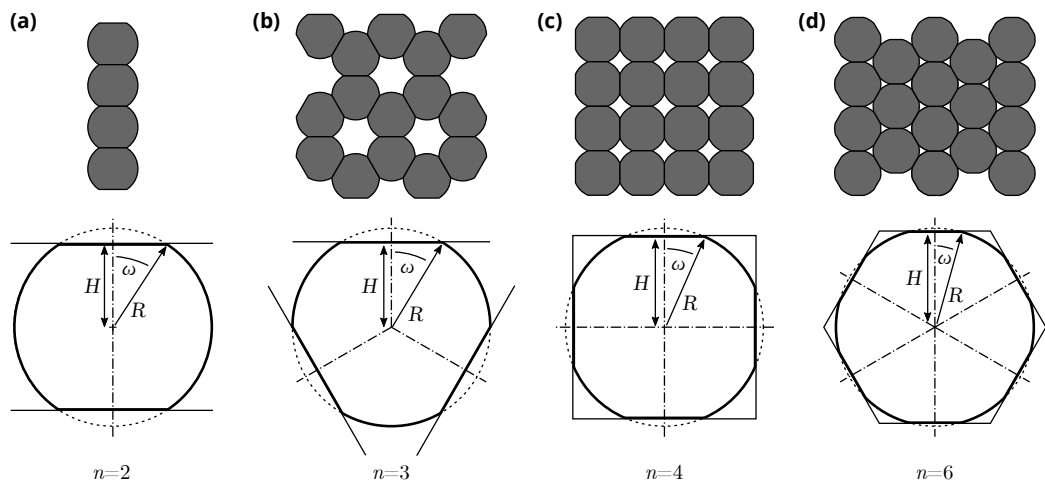


Figure 4: Geometry of a nanowire truncated by  $n = 2, 3, 4,$  or  $6$  flat surfaces that represent necks of neighboring wires. **(a)**  $n = 2$ , **(b)**  $n = 3$ , **(c)**  $n = 4$ , **(d)**  $n = 6$ .

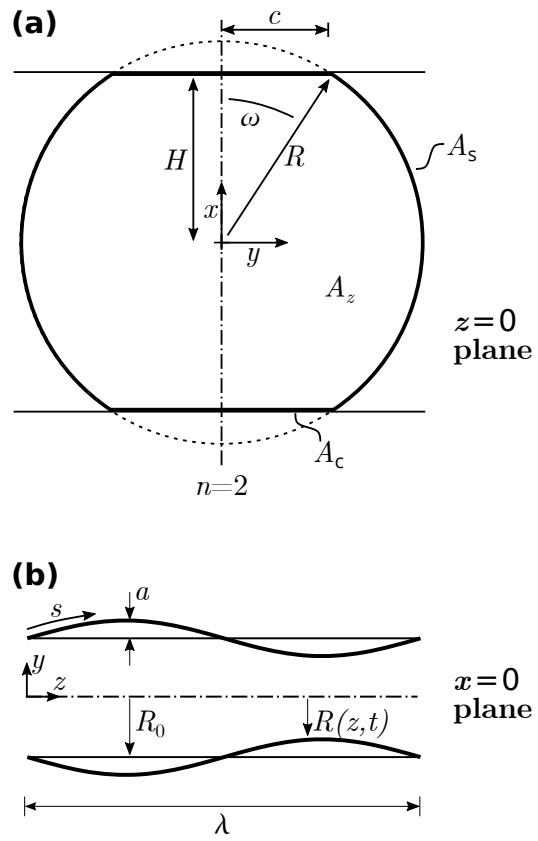


Figure 5: Cylindrical coordinate system and geometry of a perturbed nanowire. (a) The  $(x, y)$ -plane and (b) the  $(y, z)$ -plane (B).

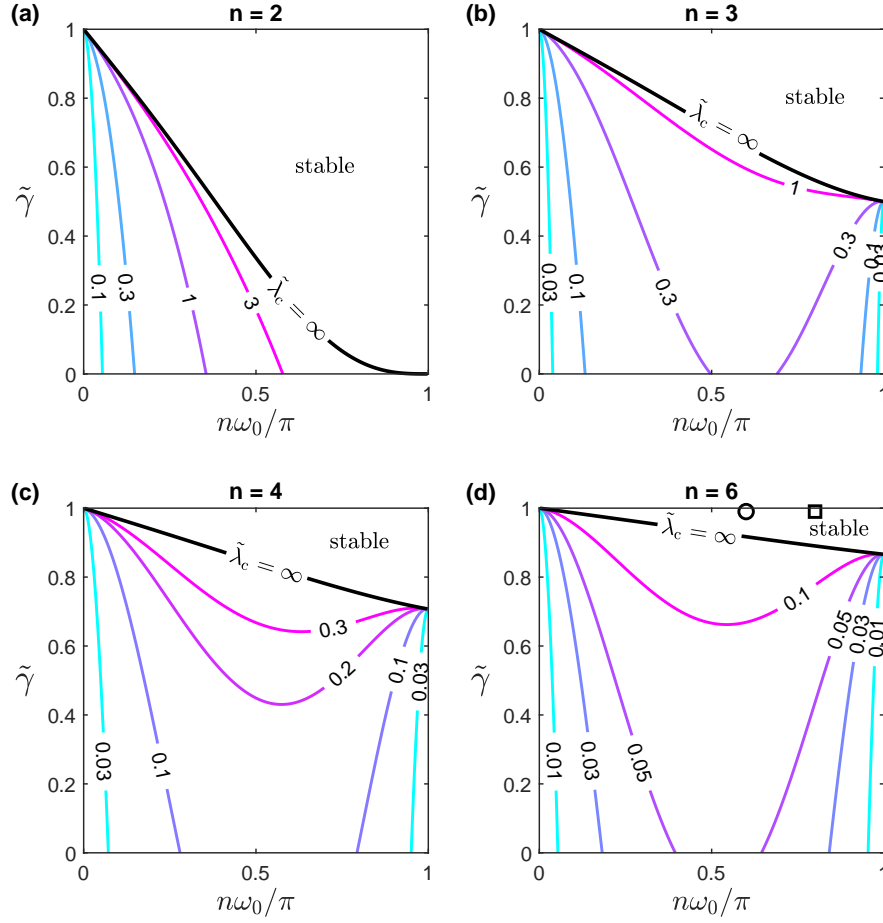


Figure 6: Contours of the critical perturbation wavelength  $\tilde{\lambda}_c = \lambda_c/(2\pi R_0)$  as a function of the surface energies  $\tilde{\gamma}$  and the initial contact angle  $\omega_0$  for a cylinder constrained by **(a)**  $n = 2$ , **(b)**  $n = 3$ , **(c)**  $n = 4$ , and **(d)**  $n = 6$  necks. The black line separates the regime in which shape stability depends on the perturbation wavelength from the regime in which the cylinder is always stable regardless of the perturbation wavelength. The circle locates our experimental material and system properties and the square that of Nouh et al. [40].

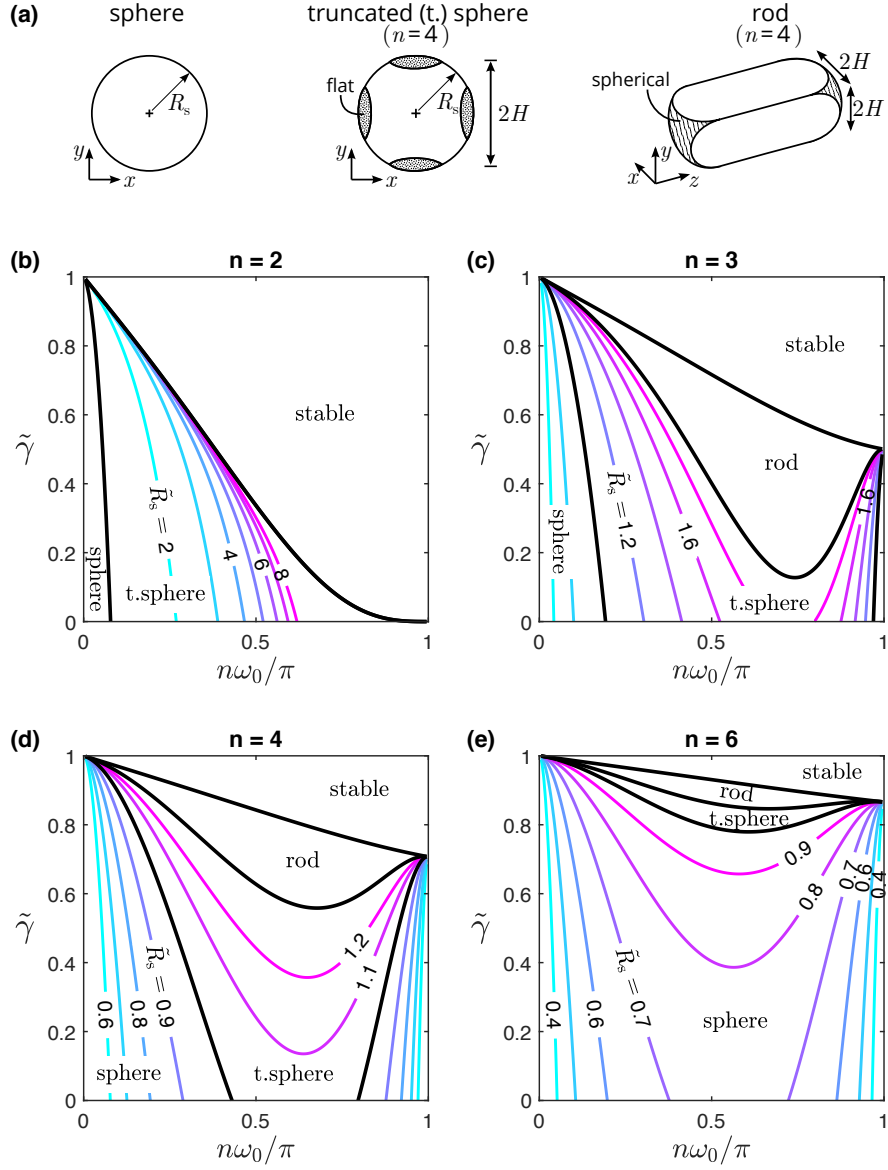


Figure 7: (a) The discrete particles emerging from pinch-off take the final form of spheres, truncated spheres (t. spheres), and rods. (b) to (e) Contours of the final, pinched-off radius of particle  $\tilde{R}_s = R_s/H$  as a function of the surface energy ratio  $\tilde{\gamma}$  and the initial contact angle  $\omega_0$  for a cylinder constrained by (b)  $n = 2$ , (c)  $n = 3$ , (d)  $n = 4$ , and (e)  $n = 6$  necks. The topologies of the final particles are marked on the maps.

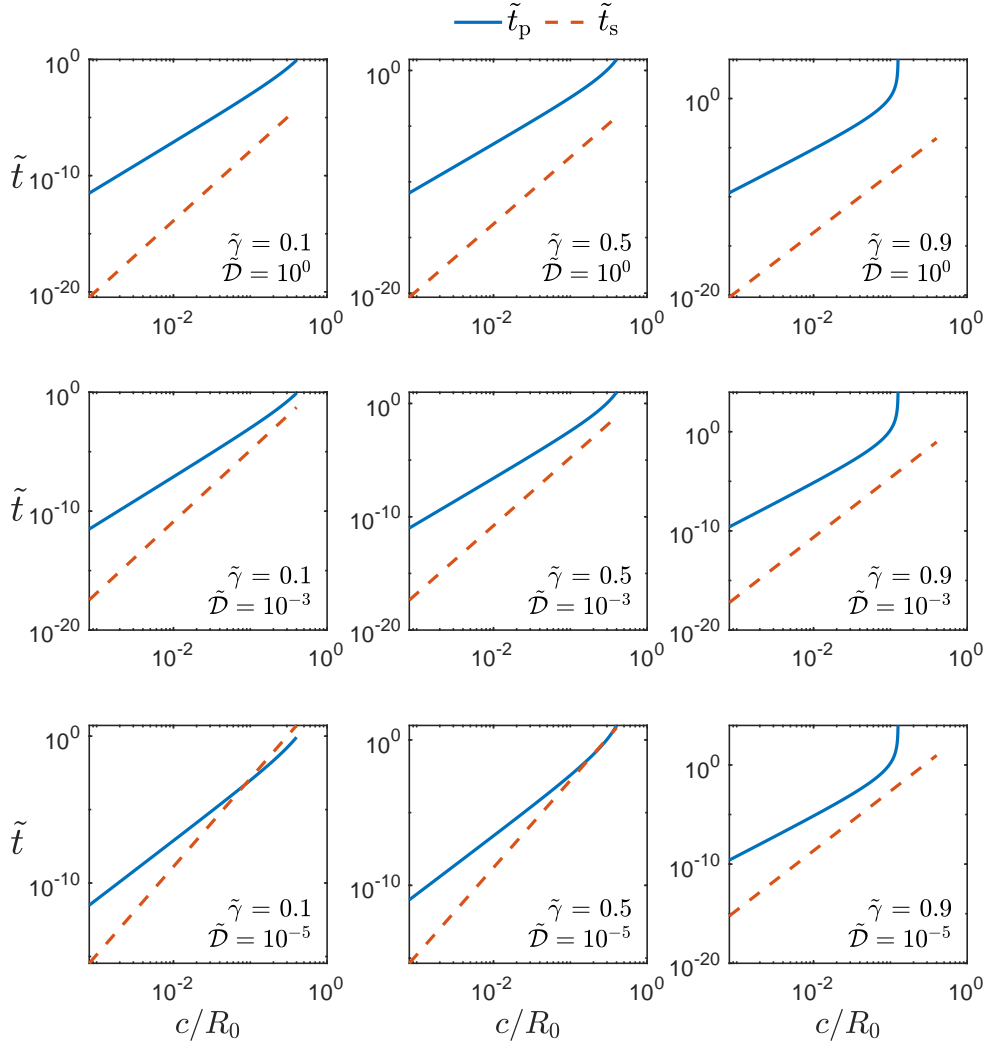


Figure 8: Pinch-off time  $\tilde{t}_p = \mathcal{D}_s \gamma_s t_p / R_0^4$  of cylinders of contact width  $c/R_0$  compared to the time  $\tilde{t}_s = \mathcal{D}_s \gamma_s t_s / R_0^4$  to sinter a row of cylinders to establish the same value of  $c/R_0$ . Predictions are shown for selected combinations of relative diffusivity  $\tilde{D} = \mathcal{D}_c / \mathcal{D}_s$  and relative surface energy  $\tilde{\gamma} = \gamma_c / \gamma_s$ .

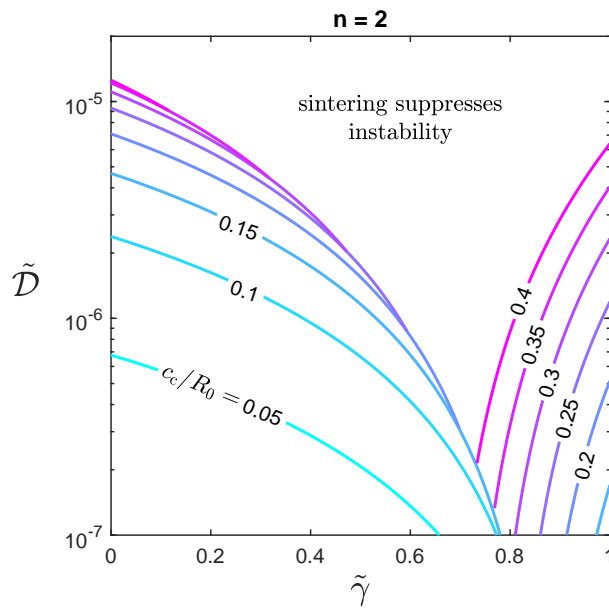


Figure 9: Contours of critical contact width  $c_c$  as a function of relative diffusivity  $\tilde{D} = \mathcal{D}_c/\mathcal{D}_s$  and relative surface energy  $\tilde{\gamma} = \gamma_c/\gamma_s$ . For  $c > c_c$ , the pinch-off time  $t_p$  is shorter than the sintering time  $t_s$ . A region exists in the map where sintering is always faster than pinch-off, regardless of the contact width  $c$ , and consequently sintering suppresses the instability.

755 **Appendix A. Stage I sintering of an array of circular cylinders**

756 Our analysis of stage I sintering of an array of circular cylinders parallels that  
 757 of Parhami et al. [51] who analyzed sintering of spheres. Consider an array of  
 758 circular cylinders of initial radius  $R_0$  with a center-to-center spacing of initial  
 759 value  $2H = 2R_0$  at time  $t = 0$ , as depicted in Fig. A.1. In stage I sintering,  
 760 the cylinders maintain a constant radius  $R_0$ , the cylinder centers approach  
 761 each other and a neck of width  $2c$  grows. The driving force is the reduction in  
 762 overall free energy associated with surface and interfacial energies. Assume  
 763 a surface energy per unit area  $\gamma_s$  of the free surface of the cylinders and an  
 764 interfacial energy per unit area  $\gamma_c$  of the contact zone. We proceed to obtain  
 765  $c(t)$ .

766 The initial cross-section of the cylinders in a unit cell at  $t = 0$  is  $A_z^0 = \pi R_0^2$ ,  
 767 and after a time  $t > 0$ , it evolves to

$$A_z = \pi R_0^2 - \frac{4}{3} \frac{c^3}{R_0} + 4hc. \quad (\text{A.1})$$

768 Conservation of mass requires  $A_z = A_z^0$ , and consequently

$$h = \frac{1}{3} \frac{c^2}{R_0} \quad (\text{A.2})$$

769 and

$$H = R_0 - \frac{c^2}{6R_0}. \quad (\text{A.3})$$

770 We use the same variational principle as defined in (30) with the definition  
 771 of  $\Delta G$  given in (18) in order to obtain  $\dot{c}$ . Assume that the dissipation in the

772 grain boundary in stage I sintering dominates that over the free surface.

773 Consequently, the dissipation potential reads

$$\Psi = \int_{A_c} \frac{j_c^2}{2\mathcal{D}_c} dA_c, \quad (\text{A.4})$$

774 where we consider unit depth along the axis of the cylinder.

775 Now obtain expressions for the surface and interface areas per unit depth.

776 For the surface area, we have

$$A_s = 2\pi R_0 - 4c + \mathcal{O}(c^2), \quad (\text{A.5})$$

777 and  $A_s^0 = 2\pi R_0$  for the initial surface area. For the contact area, we have

778  $A_c = 2c$ , and  $A_c^0 = 0$ . Upon inserting these areas into (18), we obtain

$$\Delta G = 2(\gamma_c - 2\gamma_s)c. \quad (\text{A.6})$$

779 Consider the kinematics of the diffusive flux. Conservation of mass re-

780 quires that the divergence of the flux in the grain boundary and the velocity

781 of matter into the grain boundary  $v_c$  sum to zero,

$$\nabla_s \cdot \mathbf{j}_c + v_c = 0, \quad (\text{A.7})$$

782 where  $\nabla_s$  is the surface divergence operator. This relation simplifies to

783  $\partial j_c / \partial x + v_c = 0$  for the in-plane problem. The velocity  $v_c$  is related directly



784 to the rate of change in height  $2\dot{H}$  by  $v_n = 2\dot{H}$ , where

$$\dot{H} = -\frac{c\dot{c}}{3R_0}, \quad (\text{A.8})$$

785 via (A.2) and (A.3). Consequently, the diffusive flux is

$$j_c = \frac{2c\dot{c}x}{3R_0} \quad (\text{A.9})$$

786 and (A.4) reduces to

$$\Psi = \frac{4c^5\dot{c}^2}{27\mathcal{D}_c R_0^2}. \quad (\text{A.10})$$

787 It remains to substitute (A.6) and (A.10) into (30), and to integrate with

788 respect to time  $t$  to obtain

$$c^6 = \frac{81}{2}\mathcal{D}_c R_0^2(2\gamma_s - \gamma_c)t, \quad (\text{A.11})$$

789 which is the same result as that obtained by [51] for an array of spheres,

790 except for a small difference in pre-factor.

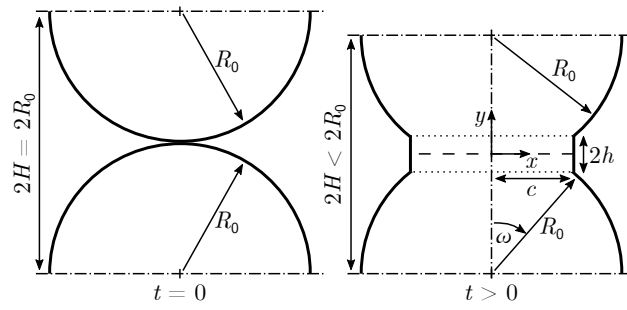


Figure A.1: Geometry of an array of circular cylinders undergoing stage I sintering.

# Supplementary Information to: Stabilization of ultrathin nanowires by self-assembly into bundles

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## 1. Chemicals

2 All chemicals used are listed in Tab. S1. Oleylamine was filtered prior to use  
3 (Millex filter, 0.45  $\mu\text{m}$ , hydrophobic PTFE). All other chemicals were used  
4 as received.

Chemical	Purity	Manufacturer
Oleylamine	80-90 % C18	Acros Organics, PA, US
Hydrogen tetrachloroaurate trihydrate ( $\text{HAuCl}_4 \cdot n\text{H}_2\text{O}$ with $n \approx 3$ )	Au content $\geq 49\%$	Acros Organics, PA, US
Triisopropylsilane	$\geq 98\%$	abcr, Germany
<i>n</i> -hexane	$\geq 99\%$	abcr, Germany
Absolute ethanol	$\geq 99.8\%$	Fisher Scientific, PA, US
Cyclooctane	$\geq 99\%$	Alfa Aesar, MA, US

Table S1: Chemicals and manufacturers.

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Kraus)

5 **2. Scattering model**

6 This section follows the work of Förster et al. [1], Sundblom et al. [2], Manet  
7 et al. [3], and Loubat et al. [4]. The total scattered intensity is the sum of  
8 the scattering contribution from spheres  $I_s$ , freely dispersed cylinders  $I_c$ , and  
9 bundled cylinders  $I_b$ . Consider each in turn.

10 *2.1. Spheres*

11 The intensity  $I_s$  scattered by a number  $n_s$  spheres is given by

$$I_s(q) = n_s(\rho_s - \rho_0)^2 P_s(q), \quad (1)$$

12 where  $\rho_s$  is the scattering length density of the sphere and  $\rho_0$  that of the  
13 solvent. The term  $P_s(q) = \langle F_s(q)^2 \rangle$  is the averaged form factor of the spheres,  
14 obtained by convoluting the form factor  $F_s$  of the spheres with a Schulz-Zimm  
15 distribution. The form factor  $F_s(q)$  of the spheres is given by

$$F_s(q) = \left( \frac{4}{3} \pi R_s^2 \right) \frac{3(\sin(qR_s) - qR_s \cos(qR_s))}{(qR_s)^3}. \quad (2)$$

16 The number of spheres  $n_s$  is related to the volume fraction of spheres  $\phi_s$  via  
17  $n_s = \phi_s / \langle V_s \rangle$ , where  $\langle V_s \rangle$  is the average volume of a sphere. The intensity of  
18 the spheres can then be written as

$$I_s(q) = \phi_s(\rho_s - \rho_0)^2 \frac{\langle F_s^2(q) \rangle}{\langle V_s \rangle} \quad (3)$$

19 *2.2. Freely dispersed nanowires*

20 Freely dispersed nanowires were modeled as cylinders of radius  $R_c$  and length  
21  $L$  with a scattered intensity of

$$I_c(q) = n_c(\rho_c - \rho_0)^2 P_c(q), \quad (4)$$

22 where  $n_c$  is the number of cylinders,  $\rho_c$  the scattering length density of the  
23 cylinder material, and  $P_c(q)$  the averaged form factor of the cylinder. The  
24 averaged form factor of the cylinder  $P_c(q)$  depends on the form factors of  
25 an infinitesimally thin cylinder  $F_{\text{thin}}(q)$  and a disk's cross-section  $F_{\text{cs}}(q)$  as  
26  $P_c(q) = F_{\text{thin}}(q) \langle F_{\text{cs}}^2(q) \rangle$ . The form factor of the cross-section  $F_{\text{cs}}(q)$  is given  
27 by

$$F_{\text{cs}}(q) = \pi R_c^2 \frac{2J_1(qR_c)}{qR_c}, \quad (5)$$

28 where  $J_1$  is the Bessel function of the first kind. The form factor of the  
 29 infinitesimally thin cylinder is given by

$$F_{\text{thin}}(q) = L^2 \left( \frac{2}{qL} \int_0^{qL} \frac{\sin(x)}{x} dx - \left( \frac{2 \sin(qL/2)}{qL} \right)^2 \right) \quad (6)$$

30 In the case of  $q \gg 1/L$ , which is valid in our scattering experiments, the  
 31 integral may be approximated by  $\int_0^{qL} \frac{\sin(x)}{x} dx \approx \frac{\pi}{2}$  so that the form factor  
 32  $F_{\text{thin}}(q)$  simplifies to

$$F_{\text{thin}}(q) = L^2 \left( \frac{\pi}{qL} - \left( \frac{2 \sin(qL/2)}{qL} \right)^2 \right) \quad (7)$$

33 In analogy to the spheres, the number of cylinders  $n_c$  is related to the volume  
 34 fraction of freely dispersed cylinders  $\phi_c$  via  $n_c = \phi_c / \langle V_c \rangle$ , where  $\langle V_c \rangle$  is the  
 35 average volume of a cylinder. The scattered intensity of the freely dispersed  
 36 cylinders can hence be written as

$$I_c(q) = \phi_c (\rho_c - \rho_0)^2 \frac{F_{\text{thin}}(q) \langle F_{\text{cs}}^2(q) \rangle}{\langle V_c \rangle}. \quad (8)$$

### 37 2.3. Bundled nanowires

38 Bundled nanowires were modeled as the average over a 2D close-packed  
 39 (hexagonal) lattice of cylinders. The scattered intensity is the one of cylin-  
 40 ders given in (8), multiplied by lattice factor of a disordered lattice  $Z(q)$  as  
 41 given by

$$I_d(q) = \phi_d (\rho_c - \rho_0)^2 \frac{F_{\text{thin}}(q) \langle F_{\text{cs}}^2(q) \rangle}{\langle V_c \rangle} Z(q). \quad (9)$$

42 The lattice factor of the disordered lattice is given by

$$Z(q) = \beta(q)G(q)Z_0(q) + (1 - \beta(q)G(q)), \quad (10)$$

43 where  $Z_0(q)$  is the lattice factor of an ideal lattice,  $\beta(q)$  accounts for disorder  
 44 in the lattice due to polydispersity of the cylinder radius, and  $G(q)$  if the  
 45 Debye-Waller factor accounting for disorder caused by thermal fluctuations.  
 46 The lattice factor of an ideal lattice of unit cell area  $A_{\text{unit}}$ , peak multiplicites  
 47  $m_{hk}$ , and peak positions  $q_{hk}$  is given by

$$Z_0(q) = \frac{1}{A_{\text{unit}}} \frac{2\pi}{q} \sum_{hk} m_{hk} L_{hk}(q, q_{hk}, \sigma). \quad (11)$$

48 Here,  $L_{hk}(q, q_{hk}, \sigma)$  is the normalized Lorentz function with a peak width of  
 49  $2\sigma$ . The term accounting for lattice disorder due to polydispersity in the  
 50 cylinder radius  $\beta(q)$  is given by

$$\beta(q) = \frac{\langle F_{cs} \rangle^2}{\langle F_{cs}^2 \rangle} \quad (12)$$

51 and the Debye-Waller factor  $G(q)$  is given by

$$G(q) = \exp(-\sigma_{\text{DW}}^2 a^2 q^2), \quad (13)$$

52 where  $\sigma_{\text{DW}}$  is the relative mean-square displacement for the positional disorder,  
 53 and  $a$  is the distance between the nearest neighbors, which is identical  
 54 to the lattice constant in the close-packed, hexagonal lattice.

### 55 **3. Additional figures**

56 The relative density (also called packing density)  $\bar{\rho}$  can be calculated for  
 57  $n \geq 3$  and is given by

$$\bar{\rho} = \frac{\cot(\pi/n)}{\cos^2 \omega_0} \left( \frac{\pi}{n} - \frac{1}{2} (2\omega_0 - \sin(2\omega_0)) \right). \quad (14)$$

58 Values of the relative density  $\bar{\rho}$  are given for example configurations in S2,  
 59 and  $\bar{\rho}$  is plotted as a function of  $n$  and  $\omega_0$  in S3a.

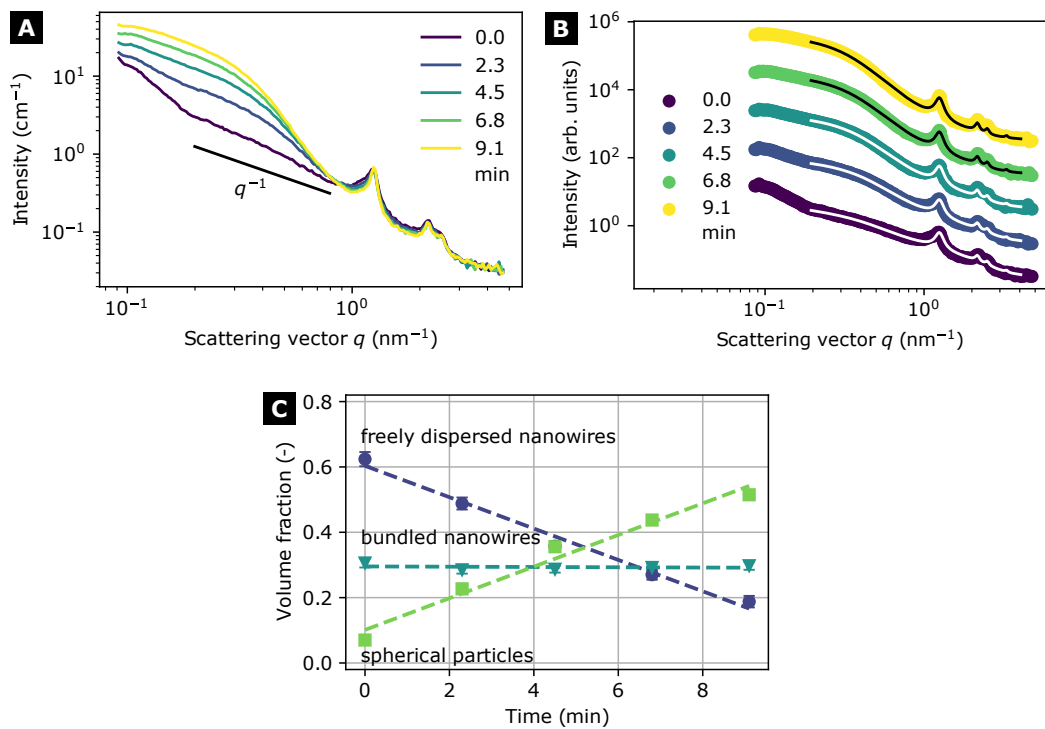


Figure S1: **(a)** Evolution of small-angle X-ray scattering from fragmenting AuNWs at 70 °C. At small  $q$ -values, the scattering signal bulges upwards, indicating that nanowires have broken-up into spheroidal particles. **(b)** Scattering models fitted to the scattering from **(a)** at selected times. Dots show experimental data points and solid lines the fits; the scattering curves are shifted vertically for better visualisation. **(c)** Volume fractions of gold in freely dispersed nanowires, bundled nanowires, and spherical particles. Error bars denote the standard error of the fits. The dashed line are linear fits.

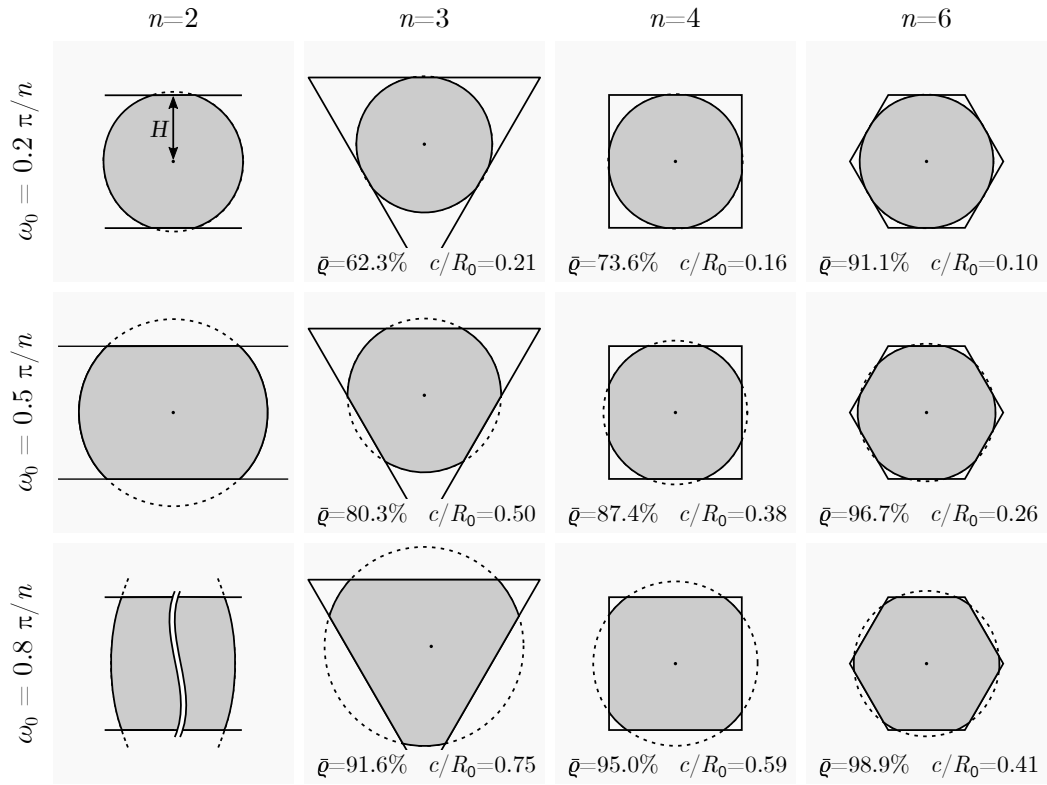


Figure S2: Example configurations a cylinder truncated by  $n$  facets at three different contact angles  $\omega_0$ . The height  $H$ , which is the distance between the cylinder's centre and the truncating surfaces, is constant among all shown configurations. For  $n \geq 3$ , the relative density (also called packing density)  $\bar{\rho}$  and the contact width  $c/R_0$  are shown.



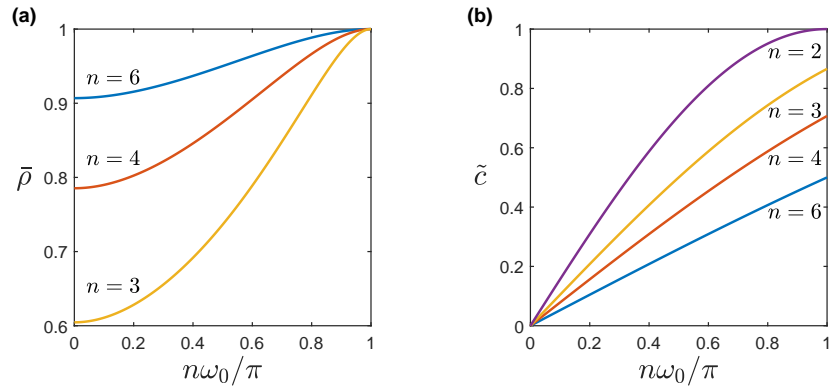


Figure S3: **(a)** Packing density  $\bar{\rho}$  as a function of the contact angle  $\omega_0$  for the tessellated arrangements of truncated cylinders as shown in Fig. S2. **(b)** The contact width  $\tilde{c} = c/R_0$  as a function of contact angle  $\omega_0$ .

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